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# Comparison of GIS-based interpolation methods for spatial distribution of soil organic carbon (SOC)



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## KEYWORDS

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GIS

**Abstract** The ecological, economical, and agricultural benefits of accurate interpolation of spatial distribution patterns of soil organic carbon (SOC) are well recognized. In the present study, different interpolation techniques in a geographical information system (GIS) environment are analyzed and compared for estimating the spatial variation of SOC at three different soil depths (0–20 cm, 20–40 cm and 40–100 cm) in Medinipur Block, West Bengal, India. Stratified random samples of total 98 soils were collected from different landuse sites including agriculture, scrubland, forest, grassland, and fallow land of the study area. A portable global positioning system (GPS) was used to collect coordinates of each sample site. Five interpolation methods such as inverse distance weighting (IDW), local polynomial interpolation (LPI), radial basis function (RBF), ordinary kriging (OK) and Empirical Bayes kriging (EBK) are used to generate spatial distribution of SOC. SOC is concentrated in forest land and less SOC is observed in bare land. The cross validation is applied to evaluate the accuracy of interpolation methods through coefficient of determination ( $R^2$ ) and root mean square error (RMSE). The results indicate that OK is superior method with the least RMSE and highest  $R^2$  value for interpolation of SOC spatial distribution.

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## 1. Introduction

Spatial variability of soil organic carbon (SOC) is an important indicator of soil quality, as well as carbon pools in the terrestrial ecosystem and it is important in ecological modeling,

environmental prediction, precision agriculture, and natural resources management (Wei et al., 2008; Zhang et al., 2012; Liu et al., 2014). Revealing the characteristics of SOC's spatial pattern will provide the basis for evaluating soil fertility, and assist in the development of sound environmental management policies for agriculture. Scientific management of SOC nutrient is important for its sustainable development in agricultural system. So, there is a need of adequate information about spatio-temporal behavior of SOC over a region. SOC measurements, however, are inherently expensive and time consuming, particularly during the installation phase, which requires soil sampling. Consequently, the number of soil sampling that is

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available in a given area is often relatively sparse and does not reflect the actual level of variation that may be present. Therefore, accurate interpolation of SOC at unsampled locations is needed for better planning and management.

Different statistical and geostatistical approaches have been used in the past to estimate the spatial distribution of SOC (Kumar et al., 2012, 2013). Classical statistics could not make out the spatial allocation of soil properties at the unsampled locations. Geostatistics is an efficient method for the study of spatial allocation of soil characteristics and their inconsistency and reducing the variance of assessment error and execution costs (Saito et al., 2005; Liu et al., 2014; Behera and Shukla, 2015). Earlier researchers have applied geospatial techniques to appraise spatial association in soils and to evaluate the geographical changeability of soil characteristics (Wei et al., 2008). Zare-mehrjardi et al. (2010), reported that ordinary kriging (OK) and cokriging methods were better than inverse distance weighting (IDW) method for prediction of the spatial distribution of soil properties. Robinson and Metternicht (2006) used three different techniques including kriging, IDW and Radial basis function (RBF) for prediction of the levels of the soil salinity, acidity and organic matter. Pang et al. (2011) reported that ordinary kriging is most common type of kriging in practice and provides an estimate of surface maps of soil properties.

Hussain et al. (2014) reported that Empirical Bayes kriging (EBK) is most suitable for spatial prediction of total dissolved solids (TSD) in drinking water. Mirzaei and Sakizadeh (2015) reported that EBK model is best of all the geostatistical models such as OK and IDW for estimation of groundwater contamination.

These five widely used interpolation methods (RBF, IDW, OK, LPI and EBK models) have led to the quest about which is most appropriate in prediction of soil organic carbon in different soil depth. Therefore, the objective of this study was to conduct a thorough comparison of the GIS based interpolation techniques for estimating the spatial distribution of SOC in Medinipur Block, West Bengal, India, and apply cross validation to evaluate the accuracy of interpolation

method through the root mean square error (RMSE) measurement.

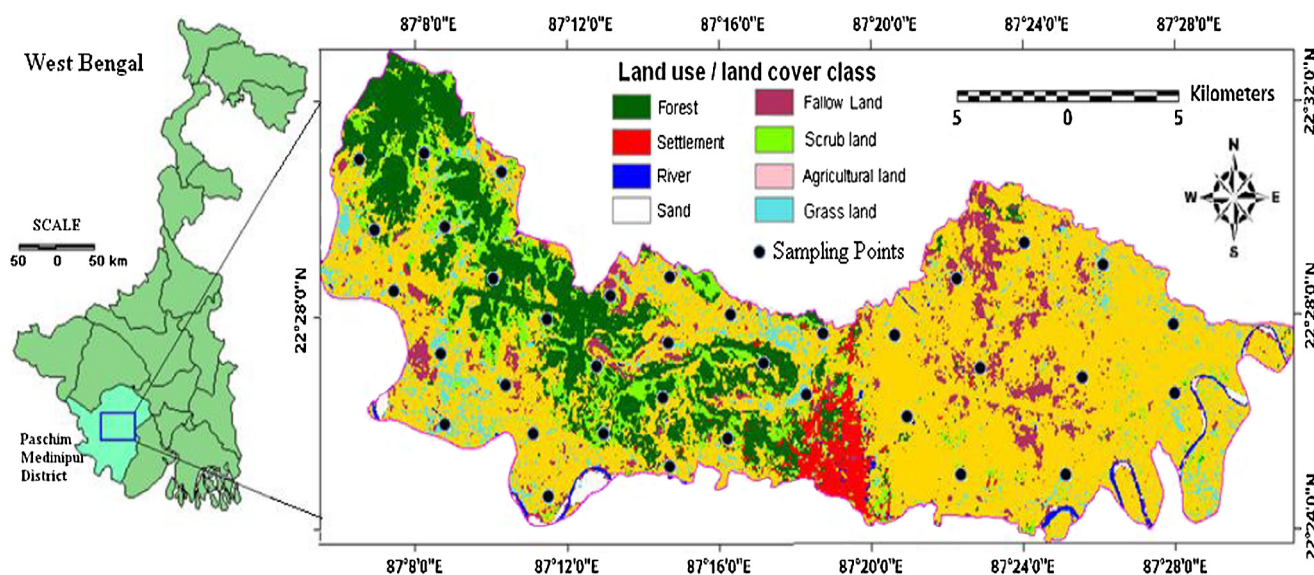
## 2. Materials and methods

### 2.1. Study area

The study was conducted in Medinipur block of Paschim Medinipur district in West Bengal (India). It is extended between  $22^{\circ}23'45''\text{N}$ – $22^{\circ}32'50''\text{N}$  latitude and  $87^{\circ}05'40''\text{E}$ – $87^{\circ}31'01''\text{E}$  longitude covering an area of 353 sq km (Fig. 1). The area is dry and the land surface of the block is characterized by red lateritic covered area, flat alluvial and deltaic plains. Extremely rugged topography is seen in the western part of the block and rolling topography is experienced in lateritic covered area (Shit et al., 2013). The maximum temperature recorded in April is  $43^{\circ}\text{C}$  and minimum temperature is  $9^{\circ}\text{C}$ . The average annual rainfall is about 1450 mm. Number of rainy days per annum is nearly about 101 days.

### 2.2. Sampling and estimate of soil properties

A pilot study was conducted to analyze the soil particles under different land use characteristics. Reconnaissance soil survey of Medinipur Block was carried out on 1:50,000 scale during 2014–2015 using the Survey of India (SOI) Toposheets as base maps. The Geo-coded Landsat 4–5 Thematic Mapper (TM) false color composite images were visually and digitally interpreted for physiographic analysis. Land use map was generated based on supervised classification technique using maximum likelihood algorithm technique in ERDAS Imagine software v9.0. The entire block has been classified into eight classes following the forest, fallow land, scrub land, agricultural land, river, sand and settlement area. To validate the classification accuracy, an error matrix table was generated and accuracy assessment analysis was performed. The study of soil profile in all physiographic units was done under different land use to develop soil–physiography relationship. Using the base



**Figure 1** Location of the study area and sampling design with land use land cover of Medinipur block derived from Landsat Thematic Mapper data.

maps, the field survey was carried out following the procedure as outlined in the [soil survey manual \(1970\)](#). The morphological features of representative pedons in each physiographic unit were studied up to a depth of 100 cm (shallow soils) and the soil samples were collected from different soil horizons for laboratory analysis.

Stratified random sampling technique was used for sampling in field during post-monsoon season. A total 98 soil samples were collated from 36 sites including agriculture (21), scrubland (16), forest (19), grassland (16), and fallow land (16) of the Medinipur block. A portable global positioning system (GPS) was used to record each sample site. In forest land use, the sampling was conducted in dense forest, degraded forest and open forest area. Undisturbed soil samples at three depths of 0–20 cm, 20–40 cm, and 40–100 cm were collected with 5 soil cores from each site and mixed well into a composite soil sample. Soil samples were air-dried and passed through a 2 mm sieve for laboratory analysis of soil texture and SOC was measured by Walkley–Black wet oxidation method ([Bao, 2000](#)).

### 2.3. Interpolation methods

In the present study, deterministic (i.e., create surfaces from measured points) and geostatistical (i.e., utilize the statistical properties of the measured points) interpolation techniques were used. In this study, a variety of deterministic interpolation techniques, including those based on either the extent of similarity (inverse distance weighted), local polynomial interpolation (LPI), degree of smoothing (radial basis functions) or geostatistical interpolation, namely ordinary kriging (OK), and Empirical Bayes (EBK) were used to generate the spatial distribution of SOC ([Johnston et al., 2001](#)).

#### 2.3.1. IDW method

The IDW is one of the mostly applied and deterministic interpolation techniques in the field of soil science. IDW estimates were made based on nearby known locations. The weights assigned to the interpolating points are the inverse of its distance from the interpolation point. Consequently, the close points are made-up to have more weights (so, more impact) than distant points and vice versa. The known sample points are implicit to be self-governing from each other ([Robinson and Metternicht, 2006](#)).

$$Z(x_0) = \frac{\sum_{i=1}^n \frac{x_i}{h_{ij}^\beta}}{\sum_{i=1}^n \frac{1}{h_{ij}^\beta}} \quad (1)$$

where  $z(x_0)$  is the interpolated value,  $n$  representing the total number of sample data values,  $x_i$  is the  $i$ th data value,  $h_{ij}$  is the separation distance between interpolated value and the sample data value, and  $\beta$  denotes the weighting power.

#### 2.3.2. LPI method

LPI fits the local polynomial using points only within the specified neighborhood instead of all the data ([Hani and Abari, 2011](#)). Then the neighborhoods can overlap, and the surface value at the center of the neighborhood is estimated as the predicted value. LPI is capable of producing surfaces that capture the short range variation ([ESRI, 2001](#)).

#### 2.3.3. RBF method

Radial basis function (RBF) predicts values identical with those measured at the same point and the generated surface requires passing through each measured point. The predicted values can vary above the maximum or below the minimum of the measured values ([Li et al., 2007, 2011](#)). RBF method is a family of five deterministic exact interpolation techniques: thin-plate spline (TPS), spline with tension (SPT), completely regularized spline (CRS), multi-quadratic function (MQ) and inverse multi-quadratic function (IMQ). RBF fits a surface through the measured sample values while minimizing the total curvature of the surface ([Johnston et al., 2001](#)). RBF is ineffective when there is a dramatic change in the surface values within short distances ([ESRI, 2001; Cheng and Xie, 2009](#)). The most widely used RBF that is CRS was selected in this study.

#### 2.3.4. OK method

Ordinary kriging method incorporates statistical properties of the measured data (spatial autocorrelation). The kriging approach uses the semivariogram to express the spatial continuity (autocorrelation). The semivariogram measures the strength of the statistical correlation as a function of distance. The range is the distance at which the spatial correlation vanishes, and the sill corresponds to the maximum variability in the absence of spatial dependence. The coefficient of determination ( $R^2$ ) was employed to determine goodness of fit ([Robertson, 2008](#)). Kriging estimate  $z^*(x_0)$  and error estimation variance  $\sigma_k^2(x_0)$  at any point  $x_0$  were, respectively, calculated as follows:

$$z^*(x_0) = \sum_{i=1}^n \lambda_i z(x_i) \quad (2)$$

$$\sigma_k^2(x_0) = \mu + \sum_{i=1}^n \lambda_i \gamma(x_0 - x_i) \quad (3)$$

where  $\lambda_i$  are the weights;  $\mu$  is the lagrange constant; and  $\gamma(x_0 - x_i)$  is the semivariogram value corresponding to the distance between  $x_0$  and  $x_i$  ([Vauclin et al., 1983; Agrawal et al., 1995](#)).

Semivariograms were used as the basic tool with which to examine the spatial distribution structure of the soil properties. Based on the regionalized variable theory and intrinsic hypotheses ([Nielsen and Wendroth, 2003](#)), a semivariogram is expressed as follows:

$$\gamma(h) = \frac{1}{2N(h)} \sum_{i=1}^{N(h)} [Z(x_i) - Z(x_i + h)]^2 \quad (4)$$

where  $\gamma(h)$  is the semivariance,  $h$  is the lag distance,  $Z$  is the parameter of the soil property,  $N(h)$  is the number of pairs of locations separated by a lag distance  $h$ ,  $Z(x_i)$ , and  $Z(x_i + h)$  are values of  $Z$  at positions  $x_i$  and  $x_i + h$  ([Wang and Shao, 2013](#)). The empirical semivariograms obtained from the data were fitted by theoretical semivariogram models to produce geostatistical parameters, including nugget variance ( $C_0$ ), structured variance ( $C_1$ ), sill variance ( $C_0 + C_1$ ), and distance parameter ( $\lambda$ ). The nugget/sill ratio,  $C_0/(C_0 + C_1)$ , was calculated to characterize the spatial dependency of the values. In general, a nugget/sill ratio  $< 25\%$  indicates strong spatial dependency and  $> 75\%$  indicates weak spatial dependency;

otherwise, the spatial dependency is moderate (Cambardella et al., 1994).

2.3.5. Empirical Bayesian kriging (EBK) method

Empirical Bayesian kriging automates the most difficult aspects through a process of subsetting and simulations. EBK process implicitly assumes that the estimated semivariogram is the true semivariogram for the interpolation region and a linear prediction that incorporates variable spatial damping. The result is a robust non-stationary algorithm for spatial interpolating geophysical corrections. This algorithm extends local trends when data coverage is good and allows for bending to a priori background mean when data coverage is poor (Knotters et al., 2010; Krivoruchko, 2012; Krivoruchko and Butler, 2013).

2.4. Cross-validation

Cross-validation technique was adopted for evaluating and comparing the performance of different interpolation methods. The sample points were arbitrarily divided into two datasets, with one used to train a model and the other used to validate the model. To reduce variability, the training and validation sets must cross over in successive rounds such that each data point is able to be validated against. The mean error (ME), the mean relative error (MRE) and the root mean square error (RMSE) for error measurement and coefficient of determination ( $R^2$  value) were estimated to evaluate the accuracy of interpolation methods. MRE is an important measure since both RMSE and ME do not provide a relative indication in reference to the actual data.

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (0_i - S_i)^2}{N}} \tag{5}$$

$$ME = \frac{\sum_{i=1}^N 0_i - S_i}{N} \tag{6}$$

$$MRE = \frac{RMSE}{\Delta} \tag{7}$$

where  $0_i$  is observed value,  $S_i$  is the predicted value,  $N$  is the Number of samples,  $\Delta$  is the range and equals the difference between the maximum and minimum observed data (see Table 1).

3. Results and discussion

3.1. Land use land cover (LULC)

Land use characteristics of the study site have been categorized into eight classes (Fig. 1). Agricultural land covers 56.91% (201 km<sup>2</sup>) of the study area and 24.76% (87 km<sup>2</sup>) area is covered by dense, degraded and open forest land. Consequently, the fallow land is covered by 8.58% (30 km<sup>2</sup>) and settlement area is enclosed by 3.57% (12 km<sup>2</sup>) of the entire study site. On the southern part of the study site Kangsabati river is flowing from western to eastern direction covering an area of 1.17% (4 km<sup>2</sup>) of the study site and the river bed deposit of sand covers an enclosed area of 2.48 km<sup>2</sup> (0.70%). The grassland covers 4.31% (15 km<sup>2</sup>) of the total land. Table 1 shows the error matrix of LULC image derived from the supervised classification technique. The overall classification accuracy and Kappa statistics were 88.00% and 0.85, respectively.

3.2. Spatial variation of SOC

Fig. 2 represents the distribution of SOC at 0–20 cm (dark shed), 20–40 cm (dark to gray shed) and 40–100 cm (very light gray shed) depth analysis. The result showed concentration of SOC is maximum in agricultural land at 0–20 cm depth and the minimum percent was recorded in fallow land and forest (Fig. 2). Consequently, SOC percent was higher in forest and agricultural land at 20–40 cm depth and minimum percent was observed in shrubs. Results also showed the highest percent of SOC in forest and grassland at 40–100 cm depth and

**Table 1** Land Use and Land Cover (LULC).

Class name	Number of pixels	Area (in km <sup>2</sup> )	Percent	Producer accuracy (%)	User accuracy (%)	Kappa ^
Built-up area	14,016	12.61	3.57	80.00	100.00	1.00
River/water bodies	4581	4.12	1.17	100.00	66.67	0.65
Sand	2762	2.48	0.7	100.00	66.67	1.00
Fallow land	33,664	30.29	8.58	75.00	100.00	0.65
Forest	64,377	57.93	16.41	85.71	85.71	0.84
Grassland	16,933	15.24	4.31	80.00	100.00	0.76
Agricultural land	223,339	201.01	56.91	100.00	83.33	0.78
Shrub land	87,838	29.48	8.35	83.33	100.00	1.00

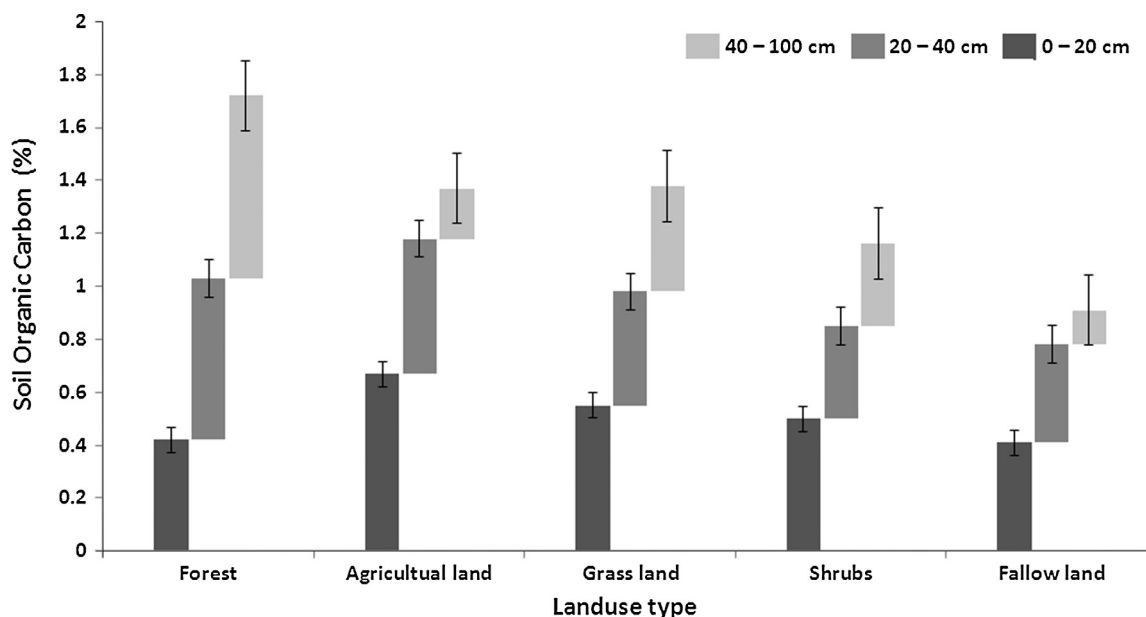
Overall classification accuracy = 88.00%.

Overall kappa statistics = 0.85.

**Table 2** Summary statistics of soil organic carbon (SOC, %) content in different soil horizons.

Soil depth (cm)	N	Mean	Median	Min	Max	SD	CV (%)	Skewness	Kurtosis
0–20	32	0.50	0.58	0.02	0.82	0.32	64.297	0.25	1.30
20–40	32	0.47	0.52	0.05	0.87	0.39	81.79	0.02	1.59
40–100	32	0.43	0.45	0.08	0.99	0.32	75.06	0.11	0.81

N = Number of samples, Min = Minimum, Max = Maximum, SD = Standard Deviation, CV = Coefficient of Variation.



**Figure 2** Characteristics of soil organic carbon in different land use categories. The error bars represent  $\pm$  one standard error.

**Table 3** Comparison of the efficiencies and errors of the interpolation methods to predict SOC.

Interpolation type	Interpolation method	Soil depth (cm)	Efficiency $R^2$	Error		
				RMSE	ME	MRE
Deterministic	IDW	0–20	0.776	0.125	0.568	0.214
		20–40	0.791	0.121	0.385	0.254
		40–100	0.808	0.145	0.645	0.210
	LPI	0–20	0.792	0.130	0.398	0.228
		20–40	0.816	0.127	0.257	0.251
		40–100	0.851	0.148	0.468	0.216
	RBF	0–20	0.742	0.176	0.845	0.268
		20–40	0.765	0.159	0.681	0.289
		40–100	0.781	0.147	0.754	0.275
Geostatistical	OK	0–20	0.918	0.110	0.110	0.158
		20–40	0.921	0.120	0.124	0.195
		40–100	0.938	0.123	0.121	0.154
	EBK	0–20	0.879	0.128	0.351	0.245
		20–40	0.848	0.127	0.364	0.235
		40–100	0.895	0.131	0.358	0.233

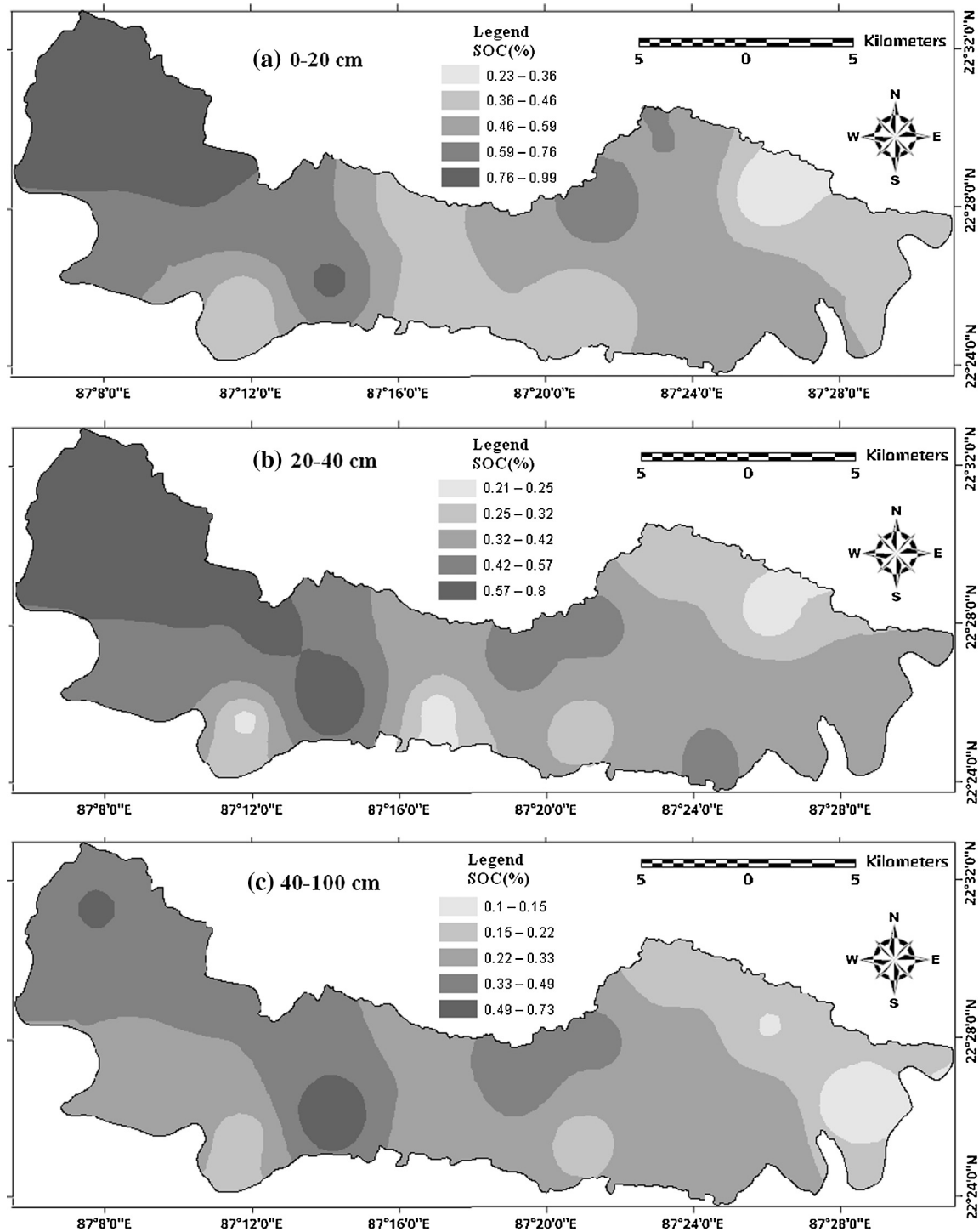
$R^2$  = coefficient of determination, RMSE = root mean square error, ME = mean error, MRE = mean relative error, IDW: inverse distance weighting, LPI: local polynomial interpolation, RBF: radial basis function, OK: ordinary kriging and EB: Empirical Bayes model.

lowest percent was observed in fallow land and agricultural land. The storage capacity of carbon among the entire forest category under consideration was significantly higher in the top layer ( $P < 0.03$ ). The present result is corroborated with previous studies by Gurumurthy et al. (2009), Sheikh et al. (2011) and Saha et al. (2012).

### 3.3. Vertical distribution of SOC

The vertical distribution of SOC percent was analyzed (Table 2). The average value of SOC was 0.50 at 0–20 cm depth, and the percent decreased with the increase of depth (Table 2).

The skewness and kurtosis coefficients are often used to describe the shape and flatness of data distribution respectively. All the data showed positive skewness, showing the concentration at lower end of data distribution. SOC content ranged from 0.02% to 0.82% (0–20 cm depth) and the allocation was positively skewed due to few high values found in the western part of the area. Average SOC content was 0.47% and 0.43% at 20–40 cm and 40–100 cm depth respectively. The results also showed positive skewness. Briefly, a good concentration of carbon sink was found in the 0–40 cm depth in all the forest soil samples in the study site. Storage of SOC in upper soil layer has been associated with the growth of root systems (Pillon, 2000) and with the quantity of aboveground biomass addition



**Figure 3** (a) Spatial distribution of SOC using IDW (inverse distance weighting), (b) spatial distribution of SOC using LPI (local polynomial interpolation), (c) spatial distribution of SOC using BRF model (radial basis function), (d) spatial distribution of SOC using EBK (Empirical Bayesian Kriging), and (e) spatial distribution of SOC using OK (ordinary kriging).

on the soil surface (Burle et al., 2005) indicating that the trees will usually increase organic carbon.

In this study, IDW, LPI, OK, EBK and RBF were used to estimate the spatial distribution of SOC. The summary statistics of the interpolation are represented in Table 3.

Fig. 3 represents the spatial distribution of SOC at three different soil depth. The characteristics of the semivariograms for SOC are abridged in Table 4. Preliminary calculations showed that all semivariograms were exponential. Semivariogram analysis indicated that SOC was best fitted to exponential

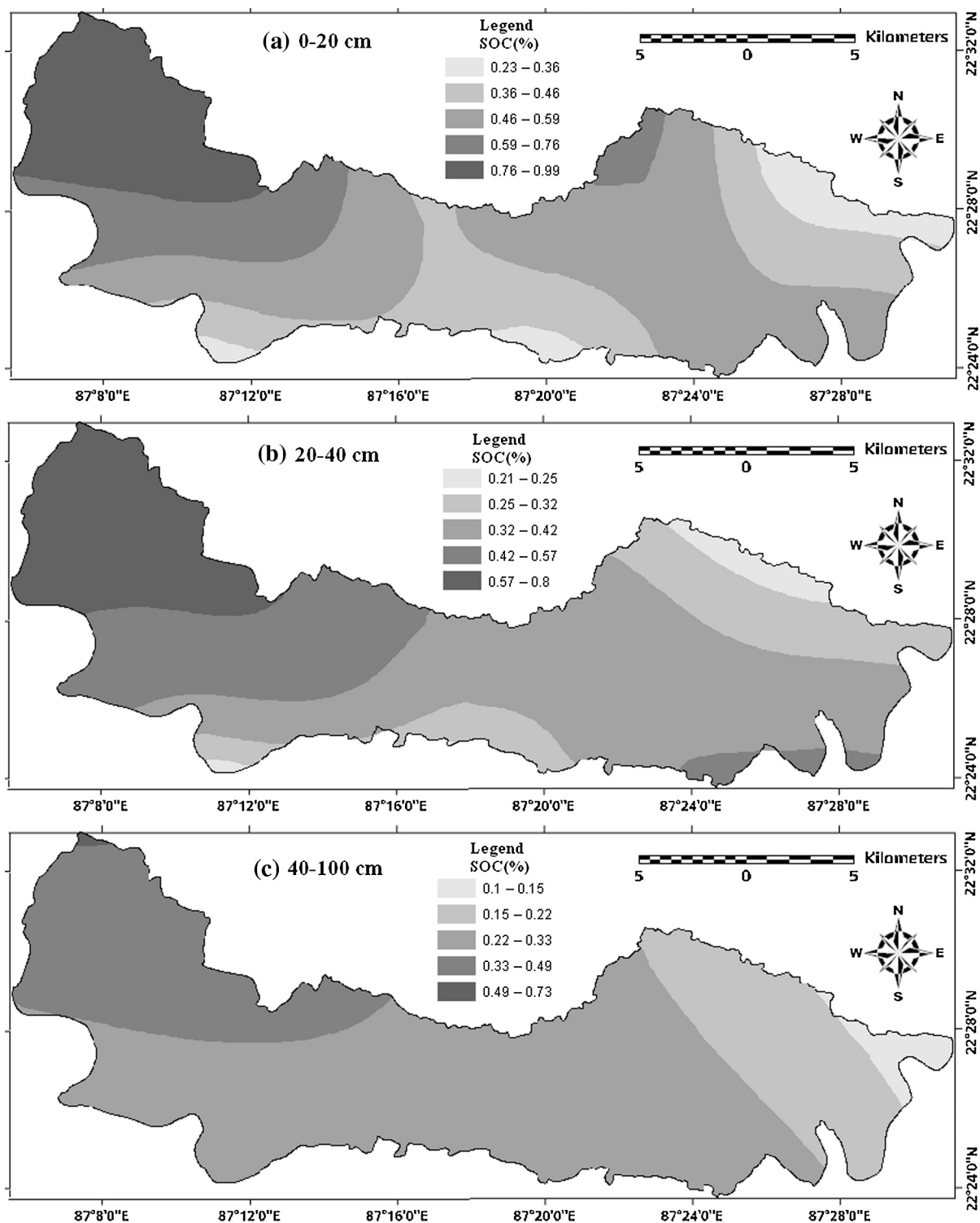


Fig. 3 (continued)

model with nugget, sill, and nugget/sill equal to 0.15, 1.10, and 0.14, respectively for 0–20 cm depth. The value of nugget, sill, and nugget/sill was recorded as 0.001, 0.97 and 0.10 respectively for 20–40 cm, and 0.001, 1.08 and 9.26 for 40–100 cm soil depth respectively.

### 3.4. Comparison of deterministic methods

Spatial distributions of SOC were analyzed in the study area obtained by deterministic methods (IDW, LPI, and RBF). The comparative results showed LPI is more accurate than

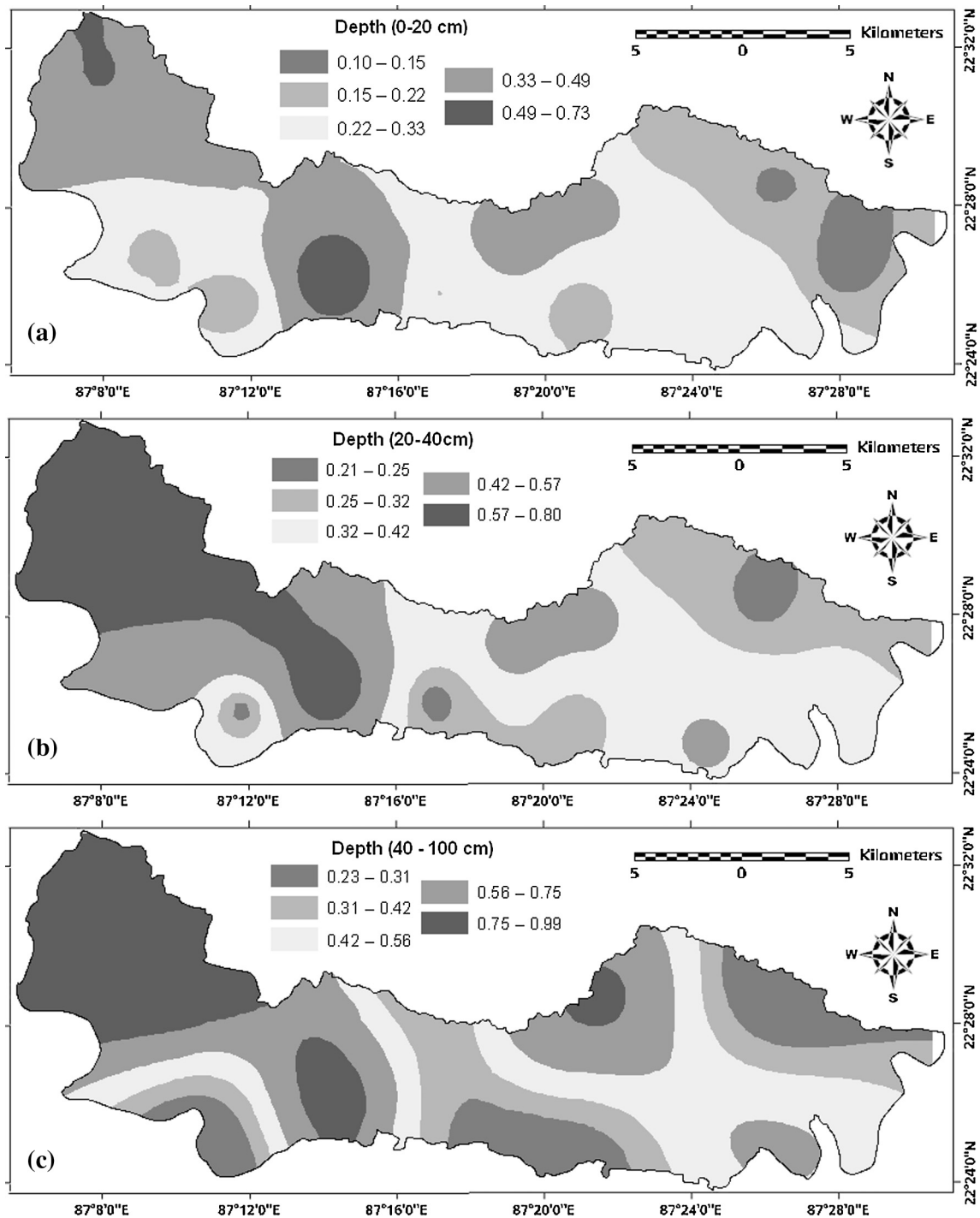


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the other two methods. The  $R^2$  value for LPI varied from 0.792, 0.816 and 0.851 for 0–20 cm, 20–40 cm and 40–100 cm respectively. The  $R^2$  value for IDW varied from 0.776, 0.791, and 0.808 for 0–20 cm, 20–40 cm and 40–100 cm respectively. However, the value of RBF showed lesser accuracy in the estimation method.

Most quantitative comparison of these three techniques was obtained through cross-validation statistics (Table 3). LPI showed RMSE of 0.125, 0.121, and 0.145 at 0–20 cm,

20–40 cm and 40–100 cm soil depth respectively. IDW resulted RMSE of 0.121–0.145 whereas RBF gave RMSE of 0.147–0.176 at different depth of SOC concentration. IDW resulted in ME of 0.385–0.645 whereas LPI gave ME of 0.257–0.468. LPI resulted in MAE of 0.216–0.251 and IDW gave RSS of 0.210–0.254. However, the result of the analysis represented that LPI is more accurate than IDW with lesser ME and smaller RMSE value. The analysis also showed IDW providing better result than RBF.



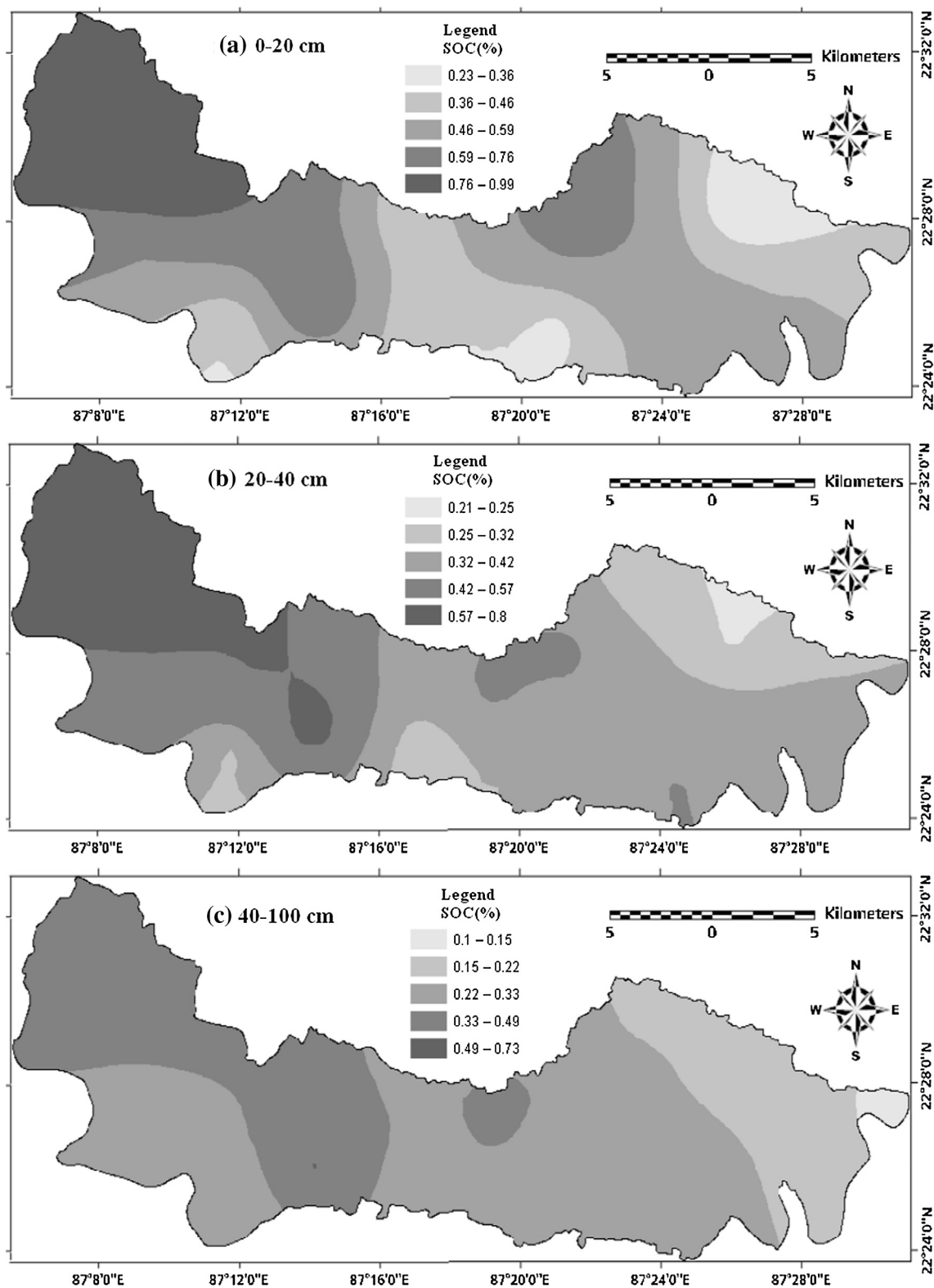


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### 3.5. Comparison of geostatistical methods

The ordinary kriging (OK) and Empirical Bayes model (EBK) are used to interpolate the spatial variability of SOC in three

soil depths (Table 3). The summary results processed by OK showed the smallest RMSE value of 0.148, 0.120 and 0.123 at 0–20 cm, 20–40 cm and 40–100 cm soil depth respectively. The Coefficient of determination ( $R^2$ ) of the model represented

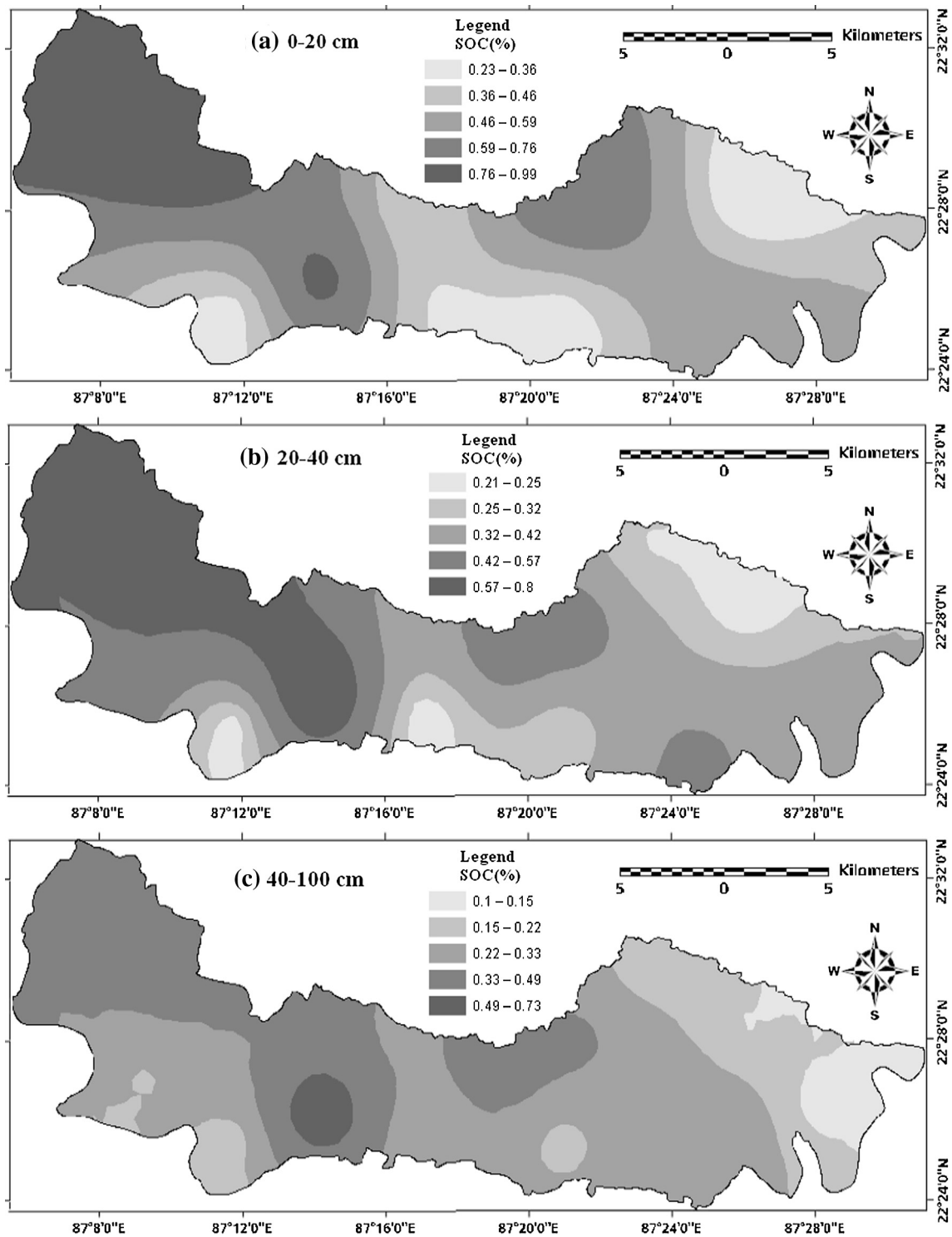


Fig. 3 (continued)

as 0.918, 0.921 and 0.938 at 0–20 cm, 20–40 cm and 40–100 cm soil depth respectively. Table 4 represents the key parameters of semivariogram model for OK.

The  $R^2$  of the model at each soil depth were greater than 0.5, indicating a good fit with the ground value. OK resulted in RMSE 0.110–0.123 whereas EBK gave 0.127–0.131. The RSS was approximately close to zero for all soil depths and

it is determined that theoretical models of SOC well reflect the spatial distribution and also corresponded strongly to the spatial correlation. OK showed the ME of 0.110–0.124 whereas EBK gave 0.351–0.364. The best results, in terms of cross validation, are achieved by OK which gave the lowest RMSE, ME and MAE. The information derived from semivariograms pointed out the reality of different spatial

**Table 4** Summary of semivariogram parameters of best-fitted theoretical model to predict soil properties and cross-validation statistics.

Soil depth (cm)	Best-fit model	Nugget ( $C_0$ )	Sill ( $C_0 + C$ )	Range (m)	Nugget/sill	$R^2$	RSS	ME	RMSE
0–20	Exponential	0.15	1.10	1.076	0.14	0.918	0.005	0.110	0.110
20–40	Exponential	0.001	0.97	1.33	0.10	0.921	0.008	0.124	0.120
40–100	Exponential	0.001	1.08	1.21	9.26	0.938	0.003	0.121	0.123

$R^2$  = coefficient of determination, RSS = residual sum square, ME = mean error, RMSE = root mean square error.

**Table 5** Summary of the performance of interpolation methods in terms of improvement over radial basis function method.

Performance soil depth (cm)	Reduction in RMSE over RBF (%)				Reduction in MRE over RBF (%)				Increase in $R^2$ over RBF (%)			
	IDW	LPI	OK	EBK	IDW	LPI	OK	EBK	IDW	LPI	OK	EBK
0–20	28.98	26.14	37.5	27.28	20.14	14.93	41.05	8.58	4.58	3.74	23.72	18.46
20–40	23.9	20.13	24.53	20.13	12.11	13.15	32.53	18.69	3.40	6.67	20.39	10.85
40–100	1.37	0.69	16.33	10.89	23.64	21.45	44.00	15.27	3.46	8.96	20.10	14.60
Average	18.08	15.65	26.12	19.43	18.63	16.51	39.19	14.18	3.81	6.45	21.40	14.63

$R^2$  = coefficient of determination, RMSE = root mean square error, ME = mean error, MRE = mean relative error, IDW: inverse distance weighting, LPI: local polynomial interpolation, RBF: radial basis function, OK: ordinary kriging, and EB: Empirical Bayes model.

dependence for collected soil properties from the field (Table 4). The proportion of nugget to sill ( $C_0/C_0 + C$ ) imitates the spatial autocorrelation (Wei et al., 2008).

### 3.6. Comparison of geostatistical and deterministic methods

The best models from the deterministic and geostatistical methods were compared to find the most suitable spatial interpolation method of the region. Assessment measures of model performance are summarized in Table 3. The superiority of IDW, LPI, OK and EBK models over RBF to predict SOC at three different soil depths was well established. To quantify the relative performance, the percentage improvement of IDW, LPI, OK and EBK was also calculated. The obtained results are shown in Table 5 and it was clearly indicated that IDW, LPI, OK and EB average decreased RMSE value of 18.08%, 15.65%, 26.12% and 19.93% respectively lower than RBF. Similarity reduction of MRE value of IDW, LPI, OK and EB was 18.63%, 16.51%, 39.19% and 14.18% respectively. The  $R^2$  value of IDW, LPI, OK and EBK models showed increase of 3.81%, 6.45%, 21.40%, and 14.63% over RBF model.

High value of coefficients of determination, and low value of RMSE and ME indicated a good match between observed and predicted SOC concentration at three different soil depths. The OK gave the lowest error (RMSE value) and highest  $R^2$  value in the spatial interpolation of three soil depths among all geostatistical methods. IDW and LPI methods gave the best results among the deterministic methods. Overall the performance of the geostatistical methods was thoroughly compared with that of the deterministic methods. The ordinary kriging was found the best among all of the methods. OK and related geostatistical techniques incorporate spatial autocorrelation and statistically optimize the weights. OK methods often give better interpolation for estimating values at unmeasured locations (Burgess and Webster, 1980; Liu et al., 2006; Nayanaka et al., 2010; Zhang et al., 2011; Mousavifard et al., 2012;

Varouchakis and Hristopulos, 2013; Venteris et al., 2014; Tripathi et al., 2015). Among the five interpolation methods, the performance of OK was best in comparison with other interpolation models. The MRE, which provided relative error of the predicted data in reference to the actual data, was also very low for OK.

## 4. Conclusion

The clear understanding of SOC distribution is the key issue for agricultural and environment management. Due to relative profusion of a variety of methods, many algorithms are presently applied, and research continues, aiming at the definition of the “best” method for delineation of spatial distribution of SOC. The methods are evaluated using efficiency and error estimates of interpolation techniques. The efficiency is assessed by coefficient of determination ( $R^2$  value), and errors are represented by the root mean square error (RMSE), mean error (ME) and mean relative error (MRE). The study shows that OK interpolation method is superior than geostatistical and deterministic methods. The performance of the exponential semi-variogram model is outstanding with OK interpolation techniques. IDW skill has the worst presentations, deriving higher RMSE and MRE than other deterministic and geostatistical methods. The study carries out at only 36 soil sampling sites over the study area of 353 km<sup>2</sup>. The interpolation could be more accurate, with more close samples and incorporation of sufficient topographical information. Finally, the results guide to the amplification of trustworthy SOC concentration maps which can significantly contribute to proper application of agricultural and ecological modeling.

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